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There are 4 basic market models: pure competition, monopolistic competition, oligopoly, and pure monopoly. Because market competition among the last 3 categories is limited, these market models imply imperfect competition. In a purely competitive market, there are large numbers of firms producing a standardized product. Market prices are determined by consumer demand; no supplier has any influence over the market price, and thus, the suppliers are price takers. Hiring English speaking models. The topic is Financial Analysis. To apply send photo and contact information to.”