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TECHNICAL PAPERS

### A Curvilinear Tool-Path Method for Pocket Machining

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
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A novel curvilinear tool-path generation method is described for planar milling of pockets. The method uses the solution of an elliptic partial differential equation boundary value problem defined on a pocket region. This mathematical function helps morph a smooth low-curvature spiral path in a pocket interior to one that conforms to the pocket boundary. This morphing leads to substantial reductions of tool wear in cutting hard metals and of machining time in cutting all metals, as experiments described here show. A variable feed-rate optimization procedure is also described. This procedure incorporates path, tool-engagement, and machine constraints and can be applied to maximize machine performance for any tool path.

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Space-filling curves tool path generation technique presented in Chap. 4 has been designed for surfaces represented in such a way that the parametric coordinates are changing within a rectangular... A curvilinear tool-path method for pocket machining. Journal of Materials Processing Technology, 125(4):709–715. Google Scholar. [10]. 3.2.2 Curvilinear tool path. 4 History. 4.1 1780-1810. There are cutting tools typically used in milling machines or machining centers to perform milling operations (and occasionally in other machine tools). They remove material by their movement within the machine (e.g., a ball nose mill) or directly from the cutter's shape (e.g., a form tool such as a hobbing cutter). A diagram of revolution ridges on a surface milled by the side of the cutter, showing the position of the cutter for each cutting pass and how it corresponds with the ridges (cutter rotation axis is perpendicular to image plane). However, there are alternative classifications according to method of control, size, purpose and power source. Mill orientation[edit]. Vertical milling machine[edit]. The curvilinear tool path, at right, reduces wasteful acceleration and deceleration by minimizing sharp corners. As the drawing shows, this path is unrecognizable as a pentagon at first, but gradually assumes the shape of the pocket as the tool spirals outward. An application developed within Boeing converts pocket shapes into efficient tool paths such as this one. These approaches to pocket machining result in tool paths made up of straight lines and tight-radius corners. The corners exaggerate the influence of acceleration and deceleration on the total cycle time. While all of the cornering may not be significant at conventional feed rates, repeatedly slowing down for corners can dramatically reduce the efficiency of a pocketing operation that uses high speed machining.